

### Single Payment



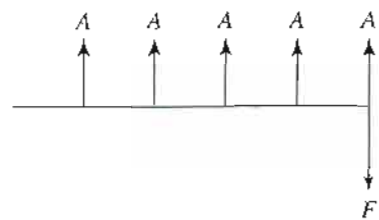
### Compound Amount:

To Find  $F$        $(F/P, i, n)$        $F = P(1 + i)^n$   
 Given  $P$

### Present Worth:

To Find  $P$        $(P/F, i, n)$        $P = F(1 + i)^{-n}$   
 Given  $F$

### Uniform Series

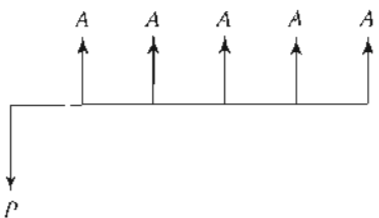


### Series Compound Amount:

To Find  $F$        $(F/A, i, n)$        $F = A \left[ \frac{(1 + i)^n - 1}{i} \right]$   
 Given  $A$

### Sinking Fund:

To Find  $A$        $(A/F, i, n)$        $A = F \left[ \frac{i}{(1 + i)^n - 1} \right]$   
 Given  $F$



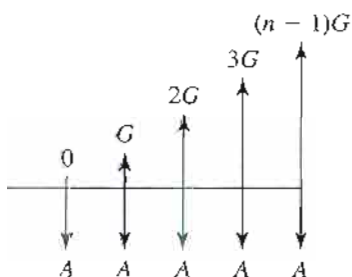
### Capital Recovery:

To Find  $A$        $(A/P, i, n)$        $A = P \left[ \frac{i(1 + i)^n}{(1 + i)^n - 1} \right]$   
 Given  $P$

### Series Present Worth:

To Find  $P$        $(P/A, i, n)$        $P = A \left[ \frac{(1 + i)^n - 1}{i(1 + i)^n} \right]$   
 Given  $A$

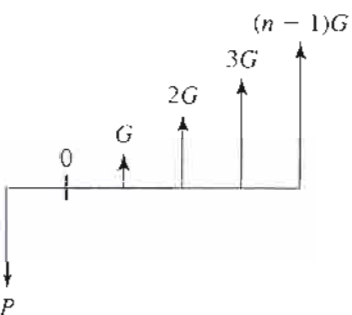
### Arithmetic Gradient



### Arithmetic Gradient Uniform Series:

To Find  $A$        $(A/G, i, n)$        $A = G \left[ \frac{(1 + i)^n - in - 1}{i(1 + i)^n - i} \right]$   
 Given  $G$

or       $A = G \left[ \frac{1}{i} - \frac{n}{(1 + i)^n - 1} \right]$



### Arithmetic Gradient Present Worth:

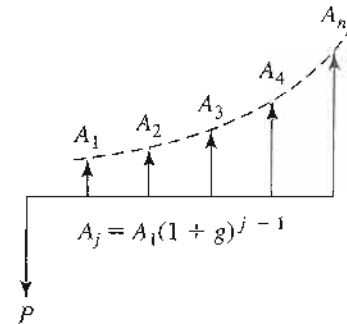
To Find  $P$        $(P/G, i, n)$        $P = G \left[ \frac{(1 + i)^n - in - 1}{i^2(1 + i)^n} \right]$   
 Given  $G$

## Geometric Gradient

Geometric Series Present Worth:

To Find  $P$   $(P/A, g, i, n)$   
 Given  $A_1, g$  When  $i = g$   $P = A_1[n(1+i)^{-1}]$

To Find  $P$   $(P/A, g, i, n)$   
 Given  $A_1, g$  When  $i \neq g$   $P = A_1 \left[ \frac{1 - (1+g)^n(1+i)^{-n}}{i - g} \right]$



## Continuous Compounding at Nominal Rate $r$

Single Payment:  $F = P[e^{rn}]$   $P = F[e^{-rn}]$

Uniform Series:  $A = F \left[ \frac{e^r - 1}{e^{rn} - 1} \right]$   $A = P \left[ \frac{e^{rn}(e^r - 1)}{e^{rn} - 1} \right]$   
 $F = A \left[ \frac{e^{rn} - 1}{e^r - 1} \right]$   $P = A \left[ \frac{e^{rn} - 1}{e^{rn}(e^r - 1)} \right]$

## Continuous, Uniform Cash Flow (One Period)

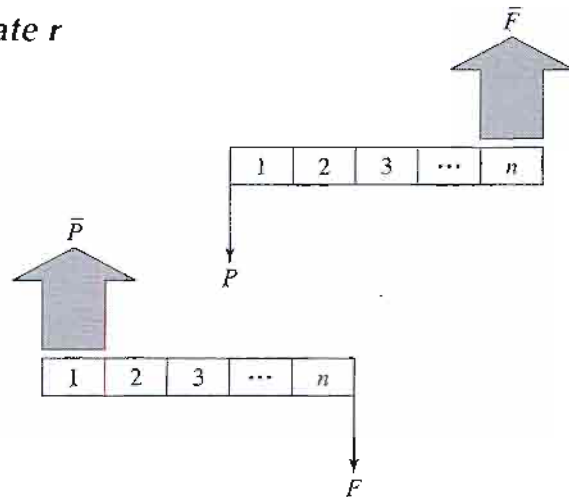
With Continuous Compounding at Nominal Rate  $r$

Present Worth:

To Find  $P$   
 Given  $\bar{F}$   $[P/\bar{F}, r, n]$   $P = \bar{F} \left[ \frac{e^r - 1}{re^{rn}} \right]$

Compound Amount:

To Find  $F$   
 Given  $\bar{P}$   $[F/\bar{P}, r, n]$   $F = \bar{P} \left[ \frac{(e^r - 1)(e^{rn})}{re^r} \right]$



## Compound Interest

$i$  = Interest rate per interest period\*.

$n$  = Number of interest periods.

$P$  = A present sum of money.

$F$  = A future sum of money. The future sum  $F$  is an amount,  $n$  interest periods from the present, that is equivalent to  $P$  with interest rate  $i$ .

$A$  = An end-of-period cash receipt or disbursement in a uniform series continuing for  $n$  periods, the entire series equivalent to  $P$  or  $F$  at interest rate  $i$ .

$G$  = Uniform period-by-period increase or decrease in cash receipts or disbursements; the arithmetic gradient.

$g$  = Uniform rate of cash flow increase or decrease from period to period; the geometric gradient.

$r$  = Nominal interest rate per interest period\*.

$m$  = Number of compounding subperiods per period\*.

$\bar{P}, \bar{F}$  = Amount of money flowing continuously and uniformly during one given period.

\*Normally the interest period is one year, but it could be something else.